



Shoubra faculty
of Engineering

2nd year Communication
2020/2021



Projects Management (PM)

إدارة المشروعات

Lecture 8

Time Management (Part3):

- Critical Path Method (CPM)
- PERT

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Dec. 2020

6) Developing the Schedule (cont'd)

Critical Path Method (CPM) or critical path analysis

- CPM is a network diag. technique used to predict total duration of project.
- You are not finished with the project until you have finished all the tasks.
- **A critical path** for a project is the series of activities that determine the **earliest time** by which the **project** can be **completed**.
➤ المسار الحرج للمشروع هو سلسلة الأنشطة التي تحدد أقرب وقت يمكن فيه إكمال المشروع
- It is the **longest path** through the network diagram and has the **least** amount of slack or float.
➤ إنه أطول مسار عبر مخطط الشبكة ويحتوي على أقل قدر من التراخي أو التعويم
- **Slack or float** is the amount of time an activity may be delayed without delaying a succeeding activity or the project finish date.
- فترة السماح أو التعويم هي مقدار الوقت الذي قد يتأخر فيه نشاط ما دون تأخير نشاط تالي أو تاريخ انتهاء المشروع

Using Critical Path to shorten project schedule

- The project manager can shorten the duration of critical-path activities by **allocating more resources** to those activities.

Some Critical Path aspects

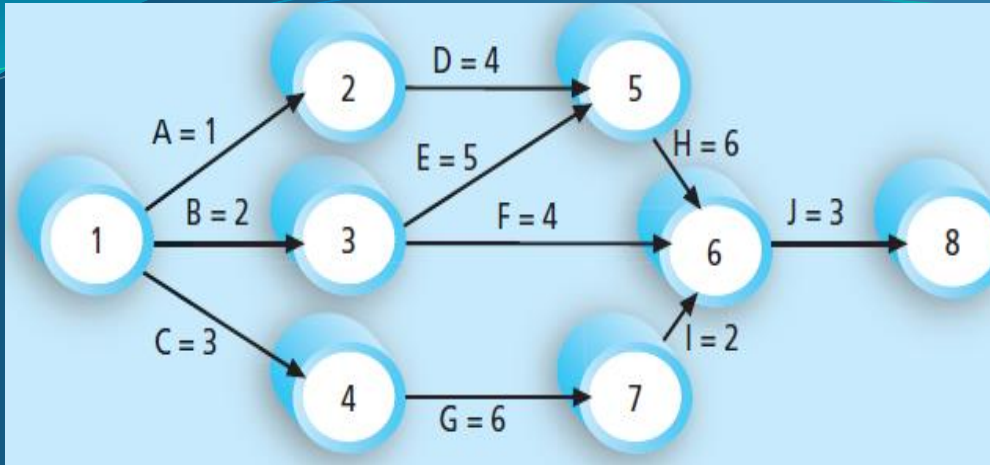
- Can there be more than one critical path for a project?

✓ Yes

- Can the critical path ever change?

✓ Yes

Calculating Critical Path



1) Determine All possible paths

A → D → H → J path1

B → E → H → J path2

B → F → J path3

C → G → I → J path4

1) All possible paths

Path1: A-D-H-J

Path2: B-E-H-J

Path3: B-F-J

Path4: C-G-I-J

2) Path length

1+4+6+3= 14 days

2+5+6+3= 16 days

2+4+3= 9 days

3+6+2+3= 14 days

3) Critical Path is: **B-E-H-J**, its length 16 days.

B, E, H, J, are critical activities, can't be delayed

Shortest time to complete the project is **16 days**

Exercise (1):

What is the **critical path** for the shown data of project Y, and what is **its length**?

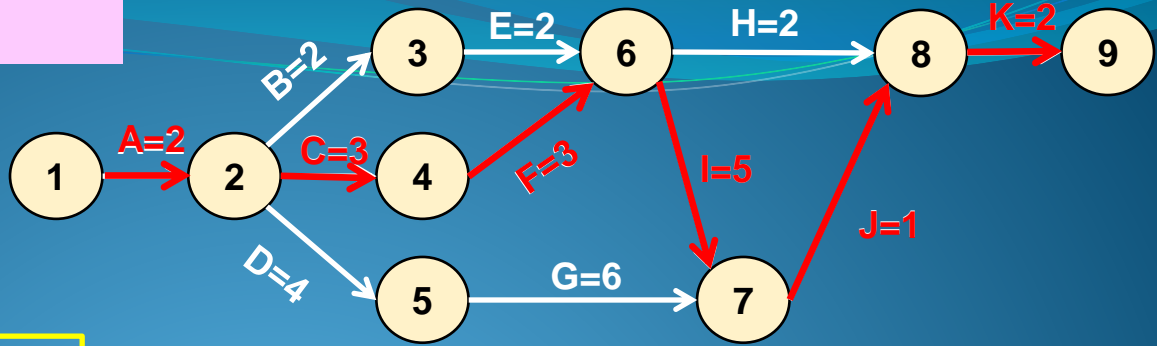
What is the **shortest time to complete this project**?

Activity	Initial Node	Final Node	Estimated Duration
A	1	2	2
B	2	3	2
C	2	4	3
D	2	5	4
E	3	6	2
F	4	6	3
G	5	7	6
H	6	8	2
I	6	7	5
J	7	8	1
K	8	9	2

Exercise (1): Solution

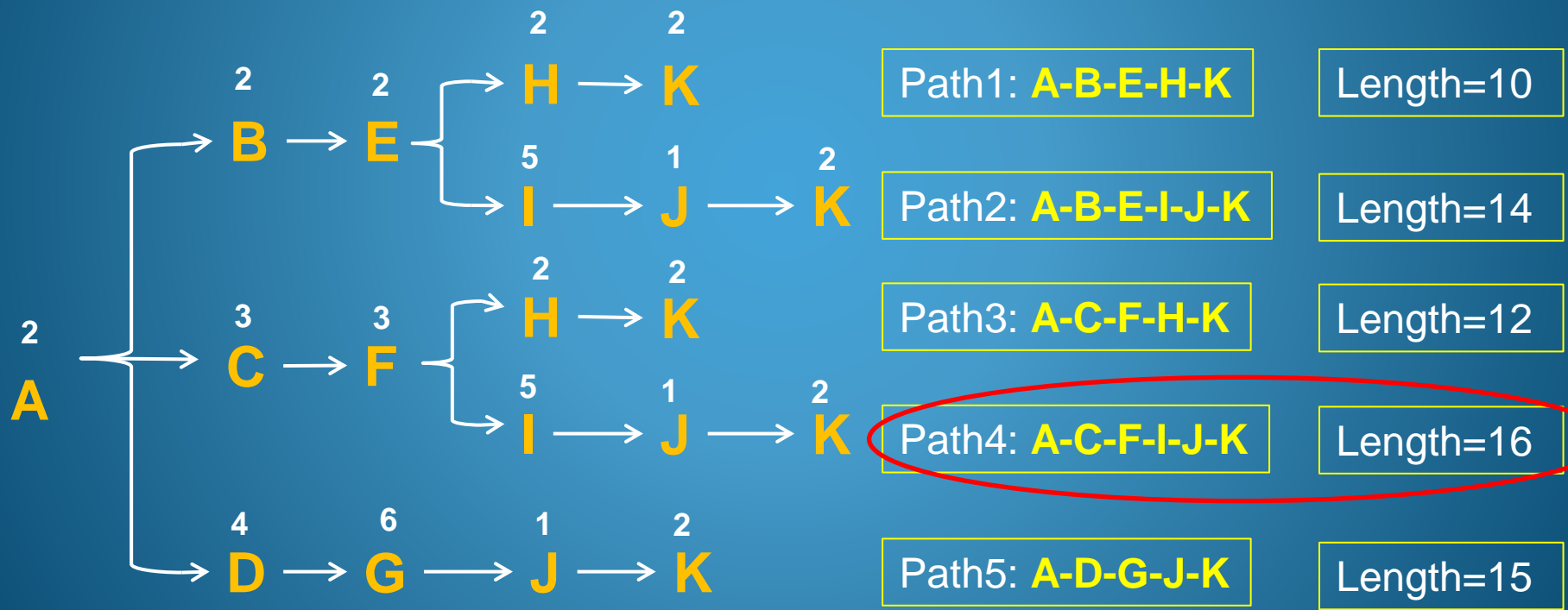
AOA network diagram

Critical path



1) Determine All possible paths

2) Lengths



3) Critical path is: **A-C-F-I-J-K** its length 16 days

A, C, F, I, J, and K are critical activities,

Shortest time to complete the project is **16 days**

Exercise

What is the **critical path** for the shown data of project Z, and what is **its length**?

What is the **shortest time to complete this project**?

Activity	Initial Node	Final Node	Estimated Duration
A	1	2	10
B	1	3	12
C	1	4	8
D	2	3	4
E	2	5	8
F	3	4	6
G	4	5	4
H	4	6	8
I	5	6	6
J	5	8	12
K	6	7	8
L	7	8	10

6) Developing the Schedule (cont'd)

Program Evaluation and Review Technique (PERT)

- **PERT** is a network analysis technique used to estimate project duration when there is a high degree of uncertainty about the activity duration.

PERT هي تقنية لتحليل الشبكة تُستخدم لتقدير مدة المشروع عندما تكون هناك درجة عالية من عدم اليقين بشأن مدة النشاط.

- PERT applies the CPM to a **weighted average duration estimate** based on **optimistic** **متفائل**, **most likely** **غالبًا**, and **pessimistic** **متشائم** estimates.

$$\text{PERT weighted average} = \frac{\text{optimistic time} + 4 * \text{most likely time} + \text{pessimistic time}}{6}$$

Ex: for an activity, optimistic time=8 workdays, pessimistic=24, most likely=10

$$\begin{aligned} \text{PERT weighted average} &= \frac{8 \text{ workdays} + 4 * 10 \text{ workdays} + 24 \text{ workdays}}{6} \\ &= 12 \text{ workdays} \end{aligned}$$

- Project team would use 12 workdays when doing critical path analysis.

Program Evaluation and Review Technique (PERT)

Example:

Use PERT technique:

- a) Draw the AOA diagram
- b) Find the critical path
- c) Calculate the shortest possible time to complete the project.

Activity name	Initial Node	Final Node	Duration		
			T_o (optimistic)	T_m (most likely)	T_p (pessimistic)
A	1	2	4	6	8
B	1	3	2	3	10
C	1	4	6	8	16
D	2	3	1	2	3
E	4	3	6	7	8
F	4	5	6	7	14
G	3	6	3	5	7
H	3	7	4	11	12
I	5	7	2	4	6
J	6	7	2	9	10

Solution

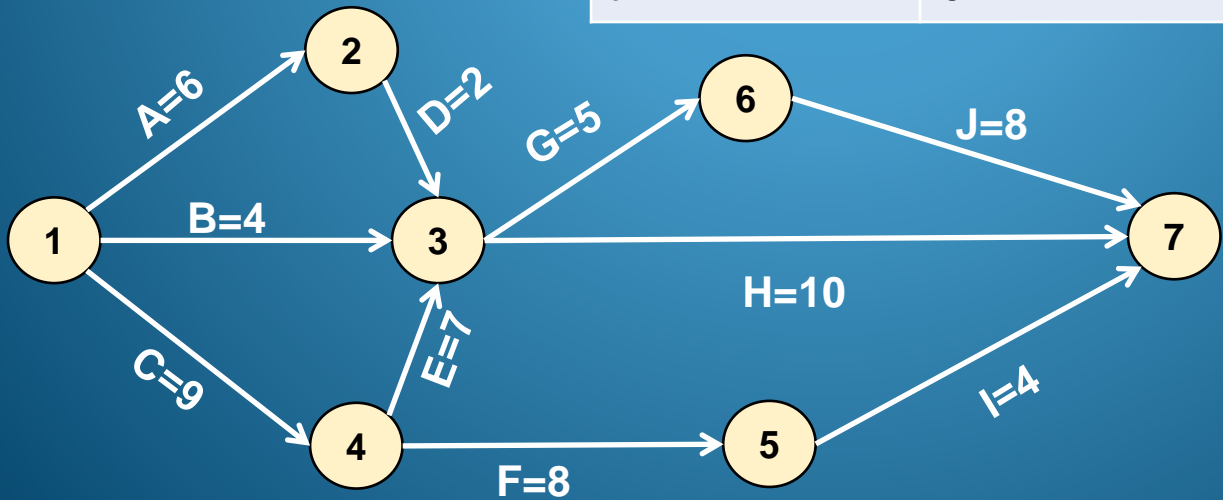
$$\text{PERT estimated duration} = \frac{T_o + (4 * T_m) + T_p}{6}$$

Activity name	Duration			Estimated duration using PERT
	T_o (optimistic)	T_m (most likely)	T_p (pessimistic)	
A	4	6	8	$\frac{4+(4*6)+8}{6} = 6$
B	2	3	10	4
C	6	8	16	9
D	1	2	3	2
E	6	7	8	7
F	6	7	14	8
G	3	5	7	5
H	4	11	12	10
I	2	4	6	4
J	2	9	10	8

Solution

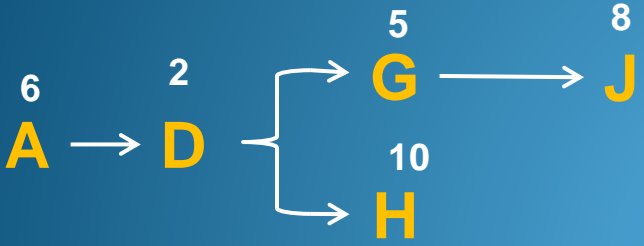
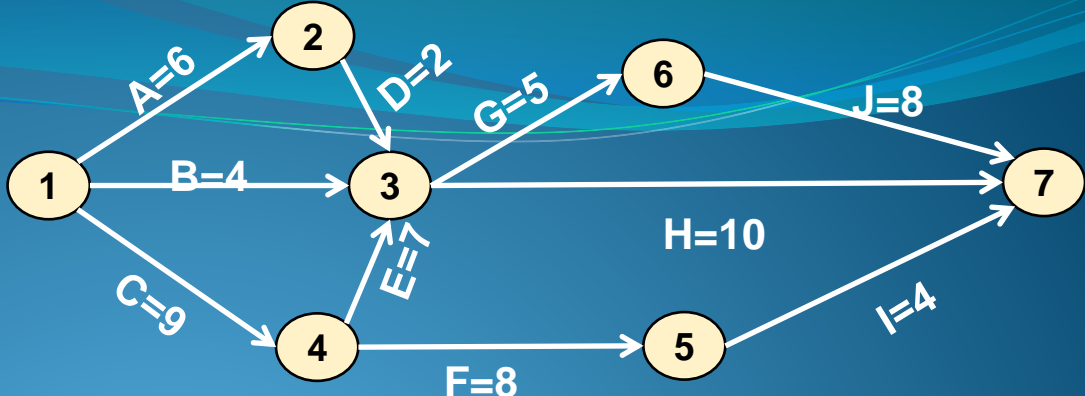
Activity name	Initial Node	Final Node	PERT duration
A	1	2	6
B	1	3	4
C	1	4	9
D	2	3	2
E	4	3	7
F	4	5	8
G	3	6	5
H	3	7	10
I	5	7	4
J	6	7	8

a) AOA diagram



Solution

b) Critical path

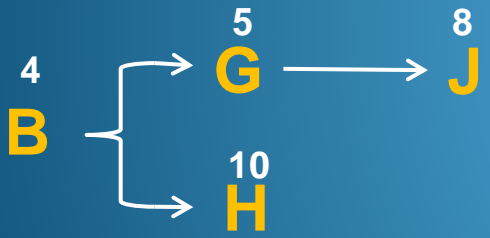


Path 1: **A-D-G-J**

Length=21

Path 2: **A-D-H**

Length=18

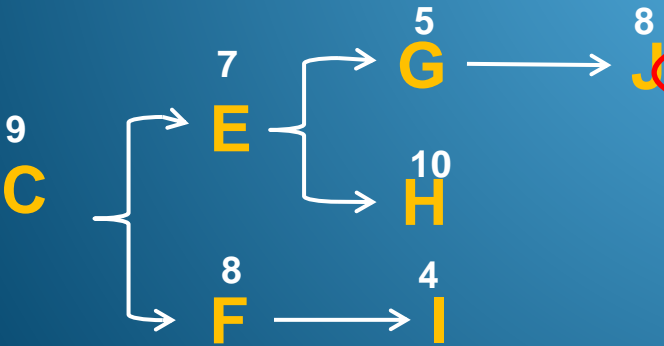


Path 3: **B-G-J**

Length=17

Path 4: **B-H**

Length=14



Path 5: **C-E-G-J**

Length=29

Path 6: **C-E-H**

Length=26

Path 7: **C-F-I**

Length=21

Critical path is: C-E-G-J
its length 29 days

Shortest time to complete the project is
29 days

Thanks for Attention